154 Homework 1, due 4/11/17

- 1. Use the chain rule to show that $\partial f/\partial x^{\mu}$ transforms as a 4-vector with lowered index. Evaluate $\partial_{\mu}(x_{\nu}x^{\nu})$ and $\partial_{\mu}x^{\mu}$.
- 2. Verify that $\phi \equiv e^{\pm ik_{\mu}x^{\mu}}$ is a plane wave solution of $\partial_{\mu}\partial^{\mu}\phi = 0$ provided that k_{μ} satisfies a certain condition and write out that condition. Suppose e.g. that $\vec{k} = (1, 2, 3)$; then what is k^0 ?
- 3. Verify that half of Maxwell's equations are solved by taking $F^{\mu\nu} = \partial^{\mu}A^{\nu} \partial^{\nu}A^{\mu}$, and that the other half then take the form $\partial_{\mu}F^{\mu\nu} = J^{\nu}$. Verify that the Lorentz force law can be written as the space component of the 4-vector equation $dp^{\mu}/d\tau = (q/c)F^{\mu\nu}u_{\nu}$, where $u^{\mu} = dx^{\mu}/d\tau$.
- 4. Verify that charge conservation can be written as $\partial_{\mu}J^{\mu}=0$, and that this is an automatic consequence / requirement of Maxwell's equations.
- 5. 2.1 in Thomson.
- 6. 2.3 in Thomson.
- 7. 2.4 in Thomson.
- 8. 2.6 in Thomson.
- 9. 2.8 in Thomson. Also, there is a typo in the process explain what it should be.
- 10. 2.12 in Thomson.